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5 The Rate Performance of 2D Material-Based Battery Electrodes May Not Be As Good As Is
6 Commonly Believed
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20 ABSTRACT: Two dimensional materials show great potential for use in battery electrodes and
21 are believed to be particularly promising for high-rate applications. However, there does not
22 seem to be much hard evidence for the superior rate-performance of 2D materials compared to
23 non-2D materials. To examine this point, we have analyzed published rate-performance data
24 for a wide range of 2D materials as well as non-2D materials for comparison. For each capacity-
25 rate curve we extract parameters which quantify performance which can then be analyzed using
26 a simple mechanistic model. Contrary to expectations, by comparing a previously proposed
27 figure of merit, we find 2D-based electrodes to be on average ~40 times poorer in terms of rate
28 performance than non-2D materials. This is not due to differences in solid-state diffusion times
29 which were similarly distributed for 2D and non-2D materials. In fact, we found the main
30 difference between 2D and non-2D materials to be that ion mobility within the electrolyte-
31 filled pores of the electrodes to be significantly lower for 2D materials, a situation which we
32 attribute to their high aspect ratios.
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45 KEYWORDS: nanosheet; cathode; anode, rate; current; model; diffusivity; diffusion
46 coefficient
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4 Over the last few years 2-dimensional (2D) materials have shown huge potential for
5 use in the number of application areas.^{1,2} Some of the most promising applications have been
6 in the field of electrochemical energy storage, particularly in the area of batteries.³ Over the
7 last decade, many papers have described using 2D materials, often in the form of synthesized
8 or exfoliated nanosheets, in both lithium- and sodium-ion batteries.⁴ While 2D materials have
9 been used in a number of roles, for example as a conductive additive,⁵ as a binder material,⁶
10 and even as a separator material,⁷ probably the most important application of 2D materials in
11 batteries has been as active materials. While the potential for graphene to effectively store
12 lithium was recognized very early,⁸ researchers eventually began to explore transition metal
13 dichalcogenide (TMD) nanosheets⁹ before more recently branching out to explore the wider
14 family of 2D materials to store both lithium and sodium.⁴ Some of these materials have shown
15 extremely high capacities. For example, black phosphorus-based electrodes have demonstrated
16 sodium ion storing capacities of approximately 2500 mAh/g,¹⁰ making it one of the most
17 promising of all battery materials.

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19 However, in addition to high capacity, it can be very important for electrode materials
20 to display good rate-performance in order to facilitate fast charging or high-power delivery.
21 Indeed, for many researchers, this is where 2D materials excel. Almost all authors claim that
22 2D materials tend to enable high rate-performance (in 53 out of 59 papers surveyed by us,
23 authors claimed their 2D material displayed good rate performance, see SI table S1). Although
24 other arguments exist (for example based on electrode morphology or conductivity, see SI table
25 S1), the most common argument is that electrodes based on 2D materials have relatively short
26 solid-state diffusion times, τ_{SSD} , leading to fast charge/discharge (this argument has also been
27 applied to nano-materials in general¹¹). The solid-state diffusion time describes the timescale
28 required for a Li or Na ion to diffuse within the particles of active material (AM), and is related
29 to the diffusion length (L_{AM}) and diffusion coefficient (D_{AM}) via $\tau_{SSD} = L_{AM}^2 / D_{AM}$. Many
30 authors argue that, for 2D materials, τ_{SSD} should be short because nanosheets tend to have small
31 L_{AM} ,¹²⁻²¹ due to their tiny size, as well as relatively large D_{AM} ,²²⁻²⁸ because of the expectation
32 that ion mobility within the inter-layer space would be higher than within 3D particles.

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34 However, the evidence for this argument is relatively sparse. A large fraction of papers
35 surveyed by us (28 out of 59 papers, see SI table S1) rely solely on reporting relatively high
36 specific capacity (mAh/g) at relatively high specific current (mA/g) as evidence of good rate
37 performance while the rest use this metric in combination with other experiments (31 out of
38 59, see SI table S1). The problem with such analysis is associated with the electrode thickness.

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3 If the electrode thickness is low, then a given specific capacity can be equivalent to a low
4 absolute amount of charge stored, while a given specific current can be achieved for a relatively
5 low absolute current. Achieving even theoretical capacity while inserting/extracting a small
6 amount of charge at low current is not good evidence of impressive rate performance. In fact,
7 real batteries need relatively thick electrodes in order to maximize charge stored as well as
8 energy density, leading to capacity-rate tradeoffs which we have previously discussed in
9 detail.²⁹ As a result, while good rate-performance might be represented by high areal capacities
10 at high areal currents, such experiments are rarely performed.³⁰

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12 In addition, even those papers that do measure D_{AM} , very rarely combine it with L_{AM} to
13 estimate τ_{SSD} . Even if τ_{SSD} is calculated, this number is of little use without context, *i.e.* what
14 are typical values of τ_{SSD} , and how big a contribution does τ_{SSD} make to the overall timescale
15 associated with charge/discharge?
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18 Thus, we believe that a detailed analysis of literature to assess whether or not 2D
19 materials do indeed display good rate performance compared to non-2D materials is required.
20 In this work we perform an extensive quantitative analysis of published rate-performance data
21 for lithium and sodium storing electrodes based on two-dimensional materials. Using a
22 published³¹ semi-empirical equation, we fit capacity-rate data, extracting parameters which can
23 be used to assess rate performance. Calculating a previously-proposed³¹ figure of merit we find
24 that 2D based electrodes have considerably poorer rate performance compared to non-2D
25 materials. In addition, we find that 2D electrodes are predominantly rate-limited by diffusion
26 effects while non-2D electrodes are limited by both diffusion and electrical effects.³¹ Using a
27 mechanistic model³¹ we find that solid-state diffusion times are similar in both 2-D and non-
28 2D electrodes. In fact, the main difference is associated with liquid diffusion within the
29 electrolyte in the porous interior of the electrode. The high aspect ratio of 2D materials can
30 significantly reduce ion mobility, dramatically increasing liquid diffusion times. This factor is
31 enough to significantly reduce rate performance, especially for thick electrodes.
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52 RESULTS AND DISCUSSION

53 *Fitting capacity-rate data*

54 While it is well-known that the capacity of battery electrodes decreases as the rate at which
55 they are charged/discharged is increased (see figure 1 for examples), using such data to quantify
56 rate performance is not straightforward. Recently,³¹ we proposed a semi-empirical equation
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3 which can fit capacity-rate data yielding three fit parameters which can be used to assess rate
4 performance:
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$$\frac{Q}{M} = Q_M \left[1 - (R\tau)^n \left(1 - e^{-(R\tau)^{-n}} \right) \right] \quad (1)$$

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10 Here Q/M is the measured specific capacity (mAh/g, generally normalised to active mass)
11 while R is the rate defined *via* the specific current (I/M) as $R = (I/M)/(Q/M)$. We note that,
12 unlike C-rate, which is defined *via* the theoretical capacity, R is calculated from the measured
13 specific capacity (at a given current). In this way, R is a measure of the actual charge/discharge
14 time. Graphs of Q/M *versus* R can be plotted (see figure 1) from typical rate data as reported in
15 nearly all battery papers. Fitting Q/M *v* R data (see figure 1) yields Q_M , τ and n , parameters
16 which can be used to quantify rate performance. The first parameter, Q_M , is the specific capacity
17 at very low rate and represents the maximum performance of the electrode material (normalised
18 in same way as Q/M). Perhaps more importantly, τ is a time constant associated with
19 charge/discharge and is a measure of the rate at which Q/M starts to fall off.^{29,31} This parameter
20 is particularly important with low time constants indicating good rate performance. Finally, n
21 is an exponent describing how rapidly Q/M decays at high rate. Low values of n indicate slow
22 decay and so good rate performance. Diffusion limited electrodes are thought to give $n \sim 0.5$
23 while electrodes whose rate performance is limited by electrical properties (*i.e.* capacitive-
24 limited) yield $n \sim 1$.³¹ Knowledge of τ and n allows a proper, quantitative assessment of the rate
25 performance of a given electrode and comparison with other electrodes.
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39 The aim of this paper is to assess the rate performance of battery electrodes based on 2D
40 materials and compare their performance to other, non-2D materials. To do this we collected
41 ~ 48 rate performance data sets from the literature for lithium- or sodium-storing electrodes
42 where the active material had a predominately 2D structure.^{10, 14, 16-19, 21-24, 26-28, 32-63} These data
43 sets encompass 28 different 2D materials grouped in the following families: graphene;
44 transition metal dichalcogenides (TMDs); other metal chalcogenides, oxides or hydroxides,
45 MXenes and other miscellaneous materials (see figure 2). We note that not all of these materials
46 are layered compounds with some of them (*e.g.* 2D LiFePO_4)⁶³ being 2D platelet-shaped
47 nanoparticles of materials with a 3D bonding scheme. In all cases, we extracted capacity-rate
48 data (see methods), calculated R and plotted Q/M *v* R . The curves were then fitted to equation
49 1 and Q_M , τ and n extracted. Some examples of fits are shown in figure 1. All fits and associated
50 data are given in the SI, figures S1-S4.
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3 The resultant fit parameters are presented in figure 2 plotted together in pairs. Each parameter
4 occupies a well-defined range: $0.3 < n < 0.8$, $10^{-3} \text{ h} < \tau < 10 \text{ h}$ and $200 \text{ mAh/g} < Q_M < 2000 \text{ mAh/g}$.
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6 The plots in figure 2 A and B show no clear correlation between n and τ or between n and Q_M .
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8 However, figure 2C suggests a possible correlation between τ and Q_M – we will discuss this in
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10 more detail below.
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13 It has previously been shown that, in addition to impacting specific capacity, electrode
14 thickness has a significant effect on rate performance.^{31, 64} Knowledge of τ , n and Q_M yields
15 an excellent opportunity to assess how the rate-performance of 2D materials depends on
16 electrode thickness. Shown in figure 3A is the time constant, τ , plotted as a function of
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18 electrode thickness. Shown in figure 3A is the time constant, τ , plotted as a function of
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20 electrode thickness, L_E . This graph shows a roughly quadratic ($\tau \propto L_E^2$) scaling over the cohort
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22 of 2D materials as was previously observed for a broader set of electrode materials.³¹ The
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24 details of this scaling will be dealt with in more detail below. Conversely, figure 3B shows no
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26 clear dependence of n on electrode thickness, although over the entire thickness range the data
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28 appears to cluster around $n \sim 0.5$. Again, this will be discussed in more detail below.
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30 The data for Q_M versus electrode thickness is shown in figure 3C. While this data is not
31 specifically associated with rate performance, Q_M represents a good estimate of the maximum
32 achievable capacity (at very low rate), and cannot be accurately obtained without performing
33 rate analysis such as that outlined here. As such, it is worth a brief discussion. This graph
34 suggests that thinner electrodes tend to display higher specific capacity, a fact that has been
35 previously observed.⁴⁰ To test this, we normalised Q_M to the theoretical specific capacity
36 (where available) and plotted this ratio versus electrode thickness in figure 3D-E. Interestingly,
37 we found a significant number of results with capacity well above the theoretical value (figure
38 3D). Although this has been previously observed, particularly for MoS_2 ,⁴¹ this data shows that
39 a number of other metal chalcogenides/oxides also display anomalously high capacities.
40 Interestingly, this cohort shows no clear dependence of normalised capacity on thickness.
41 Shown in figure 3E is normalised capacity plotted versus thickness for those data which show
42 normal behaviour (*i.e.* capacity at or below the theoretical limit). Interestingly, this data set
43 shows a clear decay of relative capacity with electrode thickness, highlighting the difficulty of
44 maintaining high specific capacity at high electrode thickness (see ref⁶⁵ for more discussion on
45 this topic).
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58 *Figure of merit for rate performance*
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In order to quantitatively assess rate performance, a Figure of Merit (FoM) is required. To achieve this, τ alone is not appropriate because it depends strongly on the electrode thickness (L_E),^{31, 66} as shown in figure 3A. We note that both figure 3A and a previously reported literature-data analysis³¹ both show an approximate scaling of $\tau \propto L_E^2$. This empirical observation is supported by a simple model recently proposed by us,³¹ which relates the charge/discharge time constant to the mechanistic factors effecting rate: the RC charging time of the electrode, the timescales associated with ion diffusion and the delay time due to the electrochemical reaction:

$$\tau = L_E^2 \left[\frac{C_{V,eff}}{2\sigma_E} + \frac{C_{V,eff}}{2\sigma_{P,E}} + \frac{1}{D_{P,E}} \right] + L_E \left[\frac{L_S C_{V,eff}}{\sigma_{P,S}} \right] + \left[\frac{L_S^2}{D_{P,S}} + \frac{L_{AM}^2}{D_{AM}} + t_c \right] \quad (2a)$$

Here $C_{V,eff}$ is the effective volumetric *capacitance* of the electrode, σ_E is the out-of-plane electrical conductivity of the electrode material, $\sigma_{P,E}$ and $\sigma_{P,S}$ are the ionic conductivities of the electrolyte within the pores of the electrode and separator respectively, $D_{P,E}$ and $D_{P,S}$ are the ionic diffusion coefficients in the electrolyte within the pores of the electrode and separator respectively, while L_S is the separator thickness. In addition, L_{AM} is the solid-state diffusion length associated with the active particles (related to particle size); D_{AM} is the solid-state Li ion diffusion coefficient within the particles such that $\tau_{SSD} = L_{AM}^2 / D_{AM}$ is the solid-state diffusion time. N.B. D_{AM} is an effective value, averaged over the relevant potential and state-of-charge ranges. Finally, t_c is a measure of the timescale associated with the electrochemical reaction once electron and ion combine at the active particle. The origin of each term in this equation has been explained in detail previously.³¹ This equation has been shown to accurately describe a wide range of experimental data and makes predictions which are consistent with observations.^{29, 31, 67}

Equation 2a has seven terms, each representing a distinct rate-limiting factor. We have previously argued that not all of these terms are important under all circumstances.³¹ For example, term 7 represents the timescale associated with the electrochemical reaction which is relatively unimportant under normal circumstances³¹ (see SI figure S5 for further justification for neglecting these two terms). Term 1 represents the contribution to the RC charging time associated with the electrical resistance of the electrode. This term can be neglected where the electrode is conductive enough (*i.e.* out of plane conductivity >1 S/m),^{31, 67} as should be the case for well-designed systems. (We accept that this will not always be the case and recommend

routine out-of-plane conductivity measurements on electrodes where quantitative rate analysis is to be performed.) In addition, we note that in porous systems, both diffusivity and ionic conductivity tend to be reduced by a factor f , compared to that in the bulk liquid (*i.e.* D_{BL} , σ_{BL}), *e.g.* $f = D_{P,E} / D_{BL} = \sigma_{P,E} / \sigma_{BL}$ (see below). In the separator, we approximate $f \approx P_S$, the separator porosity. Finally, we note our recently reported empirical observation that $C_{V,eff}$ is directly proportional to the volumetric capacity of the electrode, Q_V : $C_{V,eff} / Q_V = 28 \text{ F/mAh}$ (N.B. Q_V is the low rate capacity divided by total electrode volume: $Q_V = M_{F,A} \rho_E Q_M$, where ρ_E is the electrode density, $M_{F,A}$ is the mass fraction of active material in the electrode where Q_M , is normalised to active mass). Combining all of these observations, we can somewhat simplify equation 2a, yielding:

$$\frac{\tau}{L_E^2} \approx \left[\frac{14Q_V}{\sigma_{BL}f} + \frac{1}{D_{BL}f} + \frac{28Q_V L_S / L_E}{P_S \sigma_{BL}} + \frac{L_S^2 / L_E^2}{P_S D_{BL}} + \frac{L_{AM}^2 / L_E^2}{D_{AM}} \right] \quad (2b)$$

where Q_V should be expressed in mAh/m³ and we have neglected terms 1 and 7. These remaining terms represent the contribution of the resistance of the electrolyte within the porous electrode to the RC charging time (first term in eq 2b), the diffusion time for ions in the electrolyte within the porous interior of the electrode (second term), the contribution to the RC time constant due to the conductivity of the electrolyte in the separator (third term), the diffusion time in the separator (fourth term) and the time associated with ion diffusion within the lithium-storing particles (fifth term). This equation is useful because almost all the parameters are accessible. For a given experiment, τ , L_E , Q_V and L_S should be known in all cases while we can estimate $P_S \approx 0.5$, $\sigma_{BL} \approx 1 \text{ S/m}$ and $D_{BL} = 3 \times 10^{-10} \text{ m}^2/\text{s}$. In addition, L_{AM} is related to the particle size which can be measured while, as we will see below, f can be estimated. This leaves D_{AM} as the only unknown in equation 2b, although for some materials, literature values are available.

We note that when the electrode thickness is large compared to the solid-state diffusion length (L_{AM}) and the separator thickness (L_S), as would be the case in real electrodes, the third, fourth and fifth terms in equation 2a will become small. This means that, especially for thick electrodes, we expect $\tau \propto L_E^2$ to be a reasonable approximation, supporting the meta data mentioned above. As a result, we have proposed that L_E^2 / τ can be considered a semi-intrinsic figure of merit for rate performance in battery electrodes.³¹ Large values of this FoM indicate

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3 good rate performance, consistent with relatively short charging times, even for thick
4 electrodes.
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7 We have combined the values of τ described above with values of electrode thickness extracted
8 from the relevant publications (see methods) to calculate L_E^2 / τ for each of the 2D-based
9 electrodes described above. We have plotted the FoM as a histogram in Figure 4A. For this
10 cohort of 2D materials, we find L_E^2 / τ to vary between 10^{-14} and 10^{-11} m²/s. The logarithmic
11 mean was found to be $\langle \log(L_E^2 \tau^{-1} / \text{m}^2 \text{s}^{-1}) \rangle = -12.4$.
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19 To put these numbers into context, we reproduce data for L_E^2 / τ found by analysing a much
20 wider data set of 122 results representing lithium storing materials of all types (referred to
21 below and in the figures as “All materials”). This broader data set includes a relatively small
22 number of 2D materials. The resultant data is plotted as a histogram in Figure 4B and shows
23 the majority of L_E^2 / τ data within the wider family of lithium storing materials to vary between
24 10^{-12} and 10^{-9} m²/s with a logarithmic mean of $\langle \log(L_E^2 \tau^{-1} / \text{m}^2 \text{s}^{-1}) \rangle = -10.7$.
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31 It is clear from figures 4A-B that 2D-based electrodes have a much lower FoM compared to
32 the wider set of materials. This is a considerable difference with the shift between the
33 distributions in Figure 4A and B indicating 2D materials to have a FoM for rate performance
34 typically >10 times smaller than non-2D materials. This is clear evidence that 2D-based battery
35 electrodes have rate performance which is poorer than battery materials in general.
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40 To investigate why this might be, we plot the exponent, n , data for 2D-based electrodes reported
41 in figure 2 as a histogram (Figure 4C). This histogram shows a single peak centred around 0.5.
42 As indicated above, values of n close to 0.5 are associated with diffusion limitations. As before,
43 we can compare this data to a histogram extracted from ref³¹ which plots n -values from a much
44 broader range of battery materials, of which 2D materials are only a minor component (Figure
45 4D). This wider set of materials shows weak peaks at $n=0.5$ (representing diffusion limitations)
46 and $n=1$ (representing electrical limitations). However, the majority of data lies in the range
47 $0.5 < n < 1$ indicating a combination of diffusion and resistance limitations. This data suggests
48 that while the broader set of battery materials yield electrodes which have a range of rate
49 limiting mechanisms, 2D-based electrodes tend to be predominantly diffusion limited. We
50 believe this result is linked to the relatively low FoMs displayed by 2D-based electrodes
51 (Figure 4A).
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Analysing literature data

We believe that the low FoMs displayed by 2D-based electrodes, coupled with the fact that rate performance appears to be diffusion limited in these materials is intrinsic to 2D materials and is linked to the electrode morphology which is associated with 2D building blocks. 2D-based electrodes consist of networks of 2D sheets separated by electrolyte-filled pores (and in most cases polymer binder and a conductive additive). Ions within the electrolyte moving through the pores must travel around nanosheets and so follow a tortuous path. This means that to travel between any two points within a pore system, ions must travel much farther than would be necessary within bulk liquid. In battery research, such a reduction in ion mobility (and so diffusivity and conductivity) within pores is usually expressed *via* the factor $f = P_E / \tau_p$, where P_E is the electrode porosity and τ_p is the pore tortuosity.⁶⁸ The tortuosity is the ratio of the actual distance travelled by an ion divided by the straight line distance from start to finish and must be minimised to maximise f and so rate performance. For porous electrodes consisting of quasi-spherical particles, the tortuosity is given by the Bruggeman equation: $\tau_p = P_E^{-1/2}$, yielding $f = P_E^{3/2}$. For highly porous electrodes, P_E will be ~ 1 while 50% porosity still yields $f=0.35$, meaning tortuosity doesn't have a dramatic impact on ion mobility. However, this relationship strictly applies only to pseudo-spherical particles. Tortuosity should have a much bigger effect in pore systems associated with networks of 2D particles, especially if they are aligned in the plane of the electrode (see below). This is the reason why nanosheets have been so successful as barrier materials.⁶⁹ A number of models have estimated the effect of tortuosity on diffusion of gasses through nanosheet networks.⁷⁰ The simplest model treats networks of aligned nanosheets and for our purposes can be expressed as:⁷⁰

$$f = P_E / \tau_p = P_E \left[1 + (1 - P_E) \frac{L}{2t} \right]^{-1} \quad (3)$$

where L and t are the average nanosheet length and thickness. We note that while this expression is usually written in terms of nanosheet volume fraction (V_f), here it is more appropriate to rewrite volume fraction in terms of electrode porosity ($V_f \approx 1 - P_E$). For simplicity, we neglect the presence of binder and conductive additives. We note that equation 3 can, in principle, also be applied to aligned networks of nanosheets which have restacked during film formation, although the appropriate value of L/t is likely to be different from that of the nanosheets pre-deposition.⁷¹

Equation 3 is significant because, depending on the value of L/t , it can yield much smaller values of f than found using the Bruggeman equation. For example, taking $P_E=0.5$, for nanosheet aspect ratios of $L/t=100$, $f=0.02$ implying that in-pore diffusivities and ionic conductivities in high aspect ratio nanosheet systems are well below bulk values and significantly lower those found using $f = P_E^{3/2}$.

To test this, we note that equations 2a-b suggest that τ / L_E^2 should scale with electrode volumetric capacity, Q_V , behaviour that is hinted at in figure 2C. In Figure 5A-B, we plot τ / L_E^2 versus Q_V , for both the larger cohort representing all materials (A) as well as the narrower cohort of 2D-based electrode materials (B). In both cases, although the data sets display much scatter, a clear scaling of τ / L_E^2 with Q_V can be seen, with the 2D materials shifted upward compared to the broader data set due to their poorer rate performance. The nature of the scatter comes from the fact that both data sets contain electrodes of many different compositions and architectures, each with different electrode thickness, porosity, particle size and type. However, we would expect the bulk-electrolyte ion diffusivity (D_{BL}) and conductivity (σ_{BL}) to be similar in all cases.

The scatter makes it very difficult to quantitatively analyse the data set as a whole. However, we can get around this by considering the lower limit of each data set. In equation 2b, the first two terms are always present, simply because σ_{BL} and D_{BL} have well-defined values set by the electrolyte. However, when electrodes are thick (*i.e.* $L_E \gg L_S, L_{AM}$), the last two terms (representing ion flow in the separator and solid-state diffusion) can be neglected. This allows us to consider a lower limit to equation 2c which should act as a lower envelope to the data:

$$\left(\frac{\tau}{L_E^2} \right)_{Min} \approx \frac{14Q_V}{\sigma_{BL}f} + \frac{1}{D_{BL}f} \quad (4)$$

We would expect the broad data set representing all electrode materials to contain some highly porous materials. Thus, we can model the lower bound of that data set by taking $f=1$ and assuming reasonable values of $\sigma_{BL}=1$ S/m, $D_{BL}=3 \times 10^{-10}$ m²/s. Then, plotting equation 4 onto Figure 5A yields the grey line, which provides a reasonable match to the lower limit of the broader (grey) data set.

We have hypothesised above that the cohort of 2D materials (Figure 5B) shows poorer rate performance (ie higher τ / L_E^2) because tortuosity significantly reduces $D_{P,E}$, resulting in low

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3 values of f . Thus, we would expect the lower bound to the 2D data in Figure 5B to be
4 reproduced by again plotting Figure 5 but using a value of $f < 1$. The blue solid line in Figure
5 5B is a plot of equation 4 using the same values of σ_{BL} and D_{BL} as before but taking $f = 0.15$
6 which, according to equation 3 is associated with aligned nanosheets with aspect ratios of ~ 10 .
7 This is a reasonable value, consistent for example with gallium sulphide prepared by liquid
8 exfoliation.⁷² (We note that a similar value of f would be found for non-aligned nanosheets of
9 higher aspect ratio).

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11 For both the 2D and broader data sets, most of the data sits well above the lower bounds
12 described above. Considering equation 2a, there might be two main reasons for this scatter
13 above the lower bounds. While we would not expect σ_{BL} and D_{BL} to vary significantly over the
14 range of commonly used electrolytes, we might expect some electrodes to have lower values
15 of f if high aspect ratio nanosheets were used. Alternatively, we might expect some variation
16 in the fifth term in equation 2b if the electrode thickness (L_E) were small or the solid-state
17 diffusion time ($\tau_{SSD} = L_{AM}^2 / D_{AM}$) were large. Either factor would lead to significant increases
18 in τ / L_E^2 above its lower bound

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20 To assess the relative importance of these factors in determining the scatter in τ / L_E^2 , we plot
21 τ / L_E^2 versus L_E for both the broad data set representing all materials (figure 5C) and the set of
22 2D materials (figure 5D). In both cases, the data shows the expected scatter but also indicates
23 the general trend of appearing to decrease at low L_E but saturate at high L_E . The importance of
24 these plots is that these data sets should also be described by equation 2b. While we cannot fit
25 the data sets as a whole because of the scatter associated with variations in electrode properties,
26 we can, as before, consider lower, and in this case also upper, bounds to the data.

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28 The lower bounds to both data sets occur when Q_V and L_{AM}^2 / D_{AM} are minimised while f is
29 maximised (we assume $P_S = 0.5$, $\sigma_{BL} = 1$ S/m, $D_{BL} = 3 \times 10^{-10}$ m²/s). In line with figures 5 A-B, we
30 take $f = 1$ and 0.15 for “all materials” and “2D materials” respectively. We estimate the
31 minimum values of Q_V from the data spread in figures 5A-B to be ~ 100 and ~ 250 mAh/cm³
32 for “all materials” and “2D materials” respectively. Then, using trial and error we varied the
33 solid-state diffusion time (L_{AM}^2 / D_{AM}) until we got a reasonable lower bound to the data (solid
34 lines in figure 5 C-D) This was achieved for values of $L_{AM}^2 / D_{AM} = 3$ and 5 s for “all materials”
35 and “2D materials” respectively.

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3 We then followed a similar procedure to obtain upper bounds for the data sets in figure 5 C-D.
4 We estimate the maximum values of Q_V from the data spread in figures 5A-B to be ~ 2000 and
5 ~ 3000 mAh/cm³ for “all materials” and “2D materials” respectively. We then used trial and
6 error to find maximum values of $L_{AM}^2 / D_{AM} = 3000$ s (all) and 5000 s (2D) and minimal values
7 of $f=0.5$ (all) and 0.15 (2D) leading to reasonable upper bounds for the data sets in figure 5 C-
8 D) (dashed lines). We note that the minimal value of $f=0.15$ for 2D materials is a very rough
9 estimate. As shown in the SI (figure S6), there is simply not enough literature data for 2D-
10 based electrodes with thicknesses beyond 100 μm to properly assess the minimum value of f ,
11 other than that it lies somewhere between ~ 0.02 and 0.2. For simplicity, we take an intermediate
12 value of $f=0.15$ and interpret the similarity of maximal and minimal values of f to mean that
13 nanosheet aspect ratio does not vary over a larger range among the 2D materials under study.
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15 While these maximal and minimal values are of course approximate, they are instructive. An
16 important point is that for both “all” and 2D materials, the data is consistent with a relatively
17 small range of f -values. This implies that, for both data sets, the spread in τ / L_E^2 is not
18 predominately due to differences in tortuosity within the data set. For example, in the 2D data
19 set, this means that variations in aspect ratio or morphology do not have a large impact on
20 τ / L_E^2 . However, for both data sets the maximum and minimum values of solid-state diffusion
21 time (L_{AM}^2 / D_{AM}) are significantly different, with the maximum value being ~ 1000 times larger
22 than the minimum value in each case. This implies that, for both data sets, most of the spread
23 in τ / L_E^2 is due to variations in solid-state diffusion time. This could be down to either variation
24 in particle size (represented by L_{AM}) or solid-state diffusion coefficient (D_{AM}). Importantly, both
25 lower and upper bounds for $\tau_{SSD} = L_{AM}^2 / D_{AM}$ are similar between the broader set representing
26 all materials and the 2D materials data set. This implies that, contrary to expectations, 2D
27 materials do not have any significant advantage when it comes to solid-state diffusion as might
28 be expected due to the potential for high diffusion coefficients within the interlayer space.
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30 This means that the main differences between the data sets in figures 5 C and D is the fact that
31 while the broader set of materials have values of f roughly in the range 0.5-1, 2D materials have
32 much smaller values of f in the region of 0.15. This difference indicates that the differences in
33 rate behaviour between the two cohorts is predominately due to tortuosity in 2D based
34 electrodes which is associated with their high aspect ratio and leads to reduced ionic mobility.
35 Although this is a problem that is inherent to 2D materials, it may be resolvable simply by
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3 using 2D materials with reduced aspect ratio. Ironically, the best 2D materials for rate
4 performance in batteries may be those which are poorly exfoliated. Alternatively, it might be
5 possible to address this issue by controlling electrode morphology.
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8 9 *Electrode Morphology*

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11 It is well known that electrode morphology can significantly affect rate performance. For
12 example, Lukatskaya *et al.*⁷³ demonstrated supercapacitor electrodes with MXene nanosheets
13 organised either in a high-density, aligned arrangement or an open, highly porous structure,
14 finding very significant differences in rate performance. Similarly, Xia *et al.* showed that
15 nanocomposite supercapacitor electrodes with impressive rate performance could be obtained
16 using vertically aligned nanosheets.⁷⁴ Thus, it is worth considering the effect of morphology
17 on rate-performance in the present context.
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21 The first thing to note is that equation 2b (or 2a) incorporates the effects of morphology in a
22 number of ways. Most obvious is the factor f which determines how much the ion mobility
23 (and so diffusivity and conductivity) is reduced within the pores compared to the bulk
24 electrolyte. This factor can then be related to electrode properties *via* the Bruggeman equation
25 or using equation 3. Where the nanosheets are aligned in the plane of the film, as is relatively
26 common, equation 3 is appropriate and will lead to small values of f .
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30 Secondly, morphology is affected by particle size which is described by L_{AM} . Large particles
31 result in high solid-state diffusion times which can significantly impact rate-performance,
32 especially for thin electrodes. Finally and less obviously, morphology has an impact on the
33 volumetric capacity, Q_V , through its dependence on electrode density. Higher volumetric
34 capacity leads to larger volumetric *capacitance* and so longer RC charging times. However,
35 while the effects of morphology are incorporated in the model, that doesn't mean it is always
36 simple to implement. For example, for electrodes made of non-aligned nanosheets, it may not
37 be obvious what equation to use to estimate f . This could hamper quantitative analysis.
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41 It is worth considering the ideal morphology to minimise rate performance. In equation 2b, the
42 second and fifth terms describe the porous electrolyte diffusion time and the solid-state
43 diffusion time respectively. Both are related to morphology *via* f and L_{AM} . Clearly, both terms
44 need to be small to maximise rate performance which means f needs to be maximised (*i.e.* made
45 close to 1) and L_{AM} must be minimised. The latter condition means active particles must be
46 small which is why small nanosheets should be better than large layered crystals in terms of
47 rate performance. Maximising f means minimising tortuosity which means allowing the ions
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3 to travel along paths which are as direct as possible. The schematic in figure 6A illustrates how
4 in-plane-aligned nanosheets lead to tortuous paths.⁷⁴ Here the red and blue lines represent fast
5 and slow diffusion in the liquid and solid respectively.
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9 It has been suggested that vertically aligned nanosheets lead to fast rate performance.⁷⁴
10 However, this should not be interpreted to mean a single layer of vertical nanosheets attached
11 to the current collector at the bottom and open to the electrolyte at the top (figure 6B). In such
12 a scenario, slow diffusion within the nanosheet (blue arrow) means L_{AM} must be small to
13 maximise rate performance. However, if L_{AM} defines the electrode thickness (as in figure 6B),
14 small L_{AM} means thin electrodes and so low areal capacity and low energy density.²⁹ Rather,
15 we believe that an arrangement such as that shown in figure 6C can maximise rate performance
16 without compromising areal capacity. If the electrode consists of multiple layers of vertically
17 aligned, small nanosheets, one can envisage direct, low tortuosity paths predominately through
18 the electrolyte (red arrow) with minimal slow diffusion (blue arrow) within the nanosheets
19 themselves.
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28 We can illustrate the effect of morphology by examining three papers within the study cohort
29 which reported Li-storing electrodes based on MoS₂ nanosheets.^{18, 41, 57} In figure 6D we
30 reproduce the τ / L_E^2 versus L_E data from figure 5D for only these papers, including also the
31 lines representing plots of equation 2b. We also reproduce SEM images representing the
32 electrode morphology, extracted from these papers. The best rate performance (lowest τ / L_E^2)
33 comes from the work of Zhu *et al.*⁵⁷ who studied mixtures of MoS₂ with both nanotubes and
34 graphene. The SEM images associated with this paper reveals a number of large vertical pores
35 which allow ion transport into the interior of the electrode. Similar values of τ / L_E^2 were found
36 for the data of Liu *et al.*⁴¹ who studied MoS₂/nanotube composites. Small vertical pores can be
37 seen in the SEM image indicating ion accessibility. In addition, the nanosheets used in this
38 work were small, limiting the solid-state diffusion time. The paper of Wang *et al.*¹⁸ revealed
39 values of τ / L_E^2 somewhat higher than the previous papers indicating poorer rate performance.
40 This SEM image from this paper shows large (*i.e.* high L_{AM}), reasonably well aligned
41 nanosheets which would be expected to yield low values of f and so reduced rate performance.
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56 *Estimating Diffusion times and coefficients*

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58 Finally, the similarity between the upper and lower bounds of f for both “all materials” and 2D
59 materials data sets allows us to use this data to examine the timescale associated with diffusion
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of ions within the active particles. The solid-state diffusion time is related to both particle size and solid diffusion coefficient *via* $\tau_{SSD} = L_{AM}^2 / D_{AM}$. Equation 2b can be rearranged to give τ_{SSD} once a number of other parameters are known:

$$\tau_{SSD} = \tau - L_E^2 \left[\frac{14Q_V}{\sigma_{BL}f} + \frac{1}{D_{BL}f} + \frac{28Q_V L_S / L_E}{P_S \sigma_{BL}} + \frac{L_S^2 / L_E^2}{P_S D_{BL}} \right] \quad (5)$$

Again, τ , L_E , L_S and Q_V are known in all cases while we can estimate $P_S=0.5$, $\sigma_{BL}=1$ S/m and $D_{BL}=3 \times 10^{-10}$ m²/s. Thus, within this approximation, f is the only unknown. However as shown in figure 5 C-D, the upper and lower bounds of f are similar for each data set, allowing us to approximate f as constant in each case with average values of 0.75 (all materials) and 0.15 (2D materials). This allows us to estimate τ_{SSD} to a reasonable degree of accuracy for all sample within both cohorts. These data are plotted as histograms in figures 6 A-B for “all materials” and 2D materials respectively. We will justify the accuracy of this data below. In each case, we see relatively broad distributions in the range $1 \text{ s} < \tau_{SSD} < 10^4 \text{ s}$. Both these distributions have similar logarithmic means of $\langle \log(\tau_{SSD} / \text{s}) \rangle = 2.5$ and 2.2 for “all materials” and 2D materials respectively. Again, this indicates that, on average, 2D materials have only slightly lower solid-state diffusion times compared to other materials.

It is also useful to calculate the ratio of solid-state diffusion time to the overall time constant associated with charge/discharge (*i.e.* τ_{SSD}/τ). This ratio is of interest as it indicates how significant the contribution of solid-state diffusion is to the overall time constant. We have plotted this ratio *versus* electrode thickness in figure 7 C-D for “all materials” (C) and 2D materials (D). Because the data set is so extensive for “all materials”, figure 7C shows a well-defined trend. For low electrode thicknesses, $\tau \sim \tau_{SSD}$, meaning rate performance is dominated by solid-state diffusion within particles as might be expected. However, as electrode thicknesses increase past $\sim 10 \mu\text{m}$, τ_{SSD}/τ begins to fall. This is because, for thicker electrodes, factors such as the time associated with diffusion of ions within the electrolyte-filled porous interior of the electrode, become non negligible and eventually begin to dominate. Figure 7C implies that for electrodes thicker than a few hundred microns, solid-state diffusion is no longer dominant in most systems. Roughly the same behaviour can be seen for the 2D materials in figure 7D, although the trend is not quite as clear, probably because there are fewer data points in figure 7D compared to figure 7C. However, for 2D materials the τ_{SSD}/τ data begins to fall off at lower values of L_E compared to figure 7C. This indicates that factors such as liquid

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3 diffusion in the porous electrode becomes dominant earlier (*i.e.* at lower thicknesses) in 2D
4 systems. This is completely consistent with the fact that f (and so σ_{BL} and D_{BL}) is considerably
5 lower for 2D materials resulting in reduced ion mobility within the electrolyte filled pores.
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9 We can test the accuracy of the τ_{SSD} values for 2D materials by independently estimating the
10 solid-state diffusion time *via* $\tau_{SSD} = L_{AM}^2 / D_{AM}$, taking appropriate values of L_{AM} and D_{AM} .
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12 However, care must be taken here because, strictly speaking, L_{AM} a characteristic length
13 associated with diffusion within particles, rather than the actual particle size. Jiang *et al.*[ref⁷⁵]
14 have proposed that, for spherical particles, L_{AM} is one third of the particle radius. Assuming
15 this relationship can be applied to nanosheets, then L_{AM} is roughly one sixth of the nanosheet
16 lateral size (L). This yields $\tau_{SSD} = (L/6)^2 / D_{AM}$. To calculate τ_{SSD} , we obtained solid-state
17 diffusion coefficients (D_{AM}) from the literature for as many 2D materials as possible (see SI
18 table 3). In addition, where possible we extracted nanosheet lateral sizes (L) from the papers in
19 question. However, in many cases, mean nanosheet sizes are not given, forcing us to estimate
20 sizes from TEM/SEM images while in a few cases, it was impossible to estimate L . Thus we
21 accept that values of τ_{SSD} contained in this way will have great scope for error, partly because
22 of the crudeness of the size measurements and partly because sample-to-sample differences
23 may make the D_{AM} values inaccurate. Nevertheless, we plot values of τ_{SSD} estimated in this
24 way *versus* values estimated using equation 5 in figure 7E. Notwithstanding the uncertainty,
25 we find reasonably good agreement between values of τ_{SSD} calculated by both methods with
26 most data points sitting near the dashed line representing $y=x$. Such agreement implies that
27 equation 5 can successfully yield τ_{SSD} from standard rate performance data once f is estimated.
28 We note that for non-2D materials, f can always be estimated from the porosity *via* the
29 Bruggeman equation⁶⁸, while for 2D materials f can be estimated from the combination of
30 porosity and aspect ratio (equation 3). The exception to this good agreement is the data for
31 graphene which was calculated using $D_{AM} = 10^{-14}$ m²/s, a well-established value for graphite.⁷⁶
32 The data in figure 7E implies that the actual effective solid-state diffusion coefficient for the
33 graphene used here is significantly lower than this value. However, it is worth noting that
34 graphite comes in many forms with reported diffusion coefficients varying over four orders of
35 magnitude so perhaps this disagreement is not surprising.⁷⁷
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56 If we accept that equation 5 is reasonably accurate, then the τ_{SSD} data obtained from it can be
57 used to estimate the solid-state diffusion coefficient *via* $D_{AM} = (L/6)^2 / \tau_{SSD}$ once the particle
58 size, L is known. Using nanosheet sizes, L , estimated from each paper as described above, we
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3 calculated D_{AM} for 34 different 2D data sets encompassing both Na and Li ion batteries. These
4 values were then ordered from lowest to highest and allocated a sample number running from
5 1 for the smallest value to 34 for the largest. This data is plotted in figure 7F as sample number
6 *versus* D_{AM} . As shown in ref⁷⁸, when plotted this way, the data approximates the cumulative
7 distribution function for the data set (in this case, the distribution of solid-state diffusion
8 coefficients for 2D materials). Figure 7F implies that 2D materials tend to have Li and Na ion
9 solid-state diffusion coefficients in the range 10^{-19} - 10^{-13} m²/s. In fact, this range is quite similar
10 to that found⁷⁹ for non-2D materials where, for example, LiFePO₄ might have a diffusion
11 coefficient as low as 10^{-18} m²/s while graphite or NMC display values as high as 10^{-13} m²/s.
12 Thus, this work raises questions over the conventional wisdom that 2D materials display
13 advantages associated with fast solid-state diffusion.
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17 While there are many interesting things to note in figure 7F, we note only a few. First, three of
18 the graphene samples show very low D_{AM} , below 5×10^{-18} m²/s and probably much lower than
19 expected. In each case, these graphene samples were made by liquid phase exfoliation^{47, 48}
20 which involves sonication of graphite in solvents. We hypothesise that sonochemistry may
21 have occurred at the nanosheet edges which may hamper the entry of Li ions into the basal
22 plane.
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25 Around the middle of the distribution, there is a cluster of Li storing TMDs between sample
26 numbers 15 and 25 which the model gives diffusion coefficients in the range 2 - 7×10^{-17} m²/s.
27 This cluster contains three MoS₂ and one TiS₂ samples. According the literature, these
28 materials have Li solid-state diffusion coefficients of 15×10^{-17} m²/s (ref⁸⁰) and 4×10^{-17} m²/s
29 (ref⁸¹) respectively, in reasonably good agreement with the model predictions. Finally, it is
30 worth noting that the two highest D_{AM} values of $\sim 10^{-13}$ m²/s both come from VS₂-based
31 electrodes. These values are very similar to the value of $\sim 10^{-13}$ m²/s reported for Na ion
32 transport in VS₂.⁴⁹
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34 CONCLUSIONS

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36 In conclusion, we have extracted 48 capacity-rate data sets representing 25 different 2D
37 materials from the literature, taking care to also extract the electrode thickness, L_E in each case.
38 These were fitted using a semi-empirical equation yielding three fit parameters: the low rate
39 specific capacity, Q_M , the charge/discharge time constant, τ , and the high-rate exponent, n ,
40 parameters which can be used to assess the rate performance. This 2D data set was compared
41 to a similar, previously published data set representing a wide range of predominately non-2D
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3 materials. We found that 2D materials tended to have longer time constants than other materials
4 suggestive of poorer rate behaviour. By comparing a previously proposed figure of merit for
5 rate performance (L_E^2 / τ) we found that 2D materials are on average $\times 40$ times poorer than
6 other materials. Analysis of n shows 2D materials to be predominately rate-limited by diffusive
7 effects while other materials tend to display both diffusive and electrical limitations. Using a
8 simple model to analyse the dependence of τ / L_E^2 on both L_E and the low rate volumetric
9 capacity, Q_V , we found the range of solid-state diffusion times to be similar for both 2D and
10 non-2D materials. However, we found the ionic mobility within the electrolyte-filled porous
11 interior of the electrode to be significantly lower for 2D materials compared to non-2D
12 materials. We believe this to be a consequence of common morphologies of 2D-based
13 electrodes where ions are forced to follow tortuous paths as they travel through the electrodes.
14 However, we suggest that alternative morphologies exist which yield much less tortuous paths
15 and could result in much better rate performances.

30 METHODS

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32 Capacity-rate data were extracted from published papers using the “digitizer” function in
33 Origin. Charge/discharge rate is generally expressed *via* current or C-rate. These parameters
34 were converted to rate, R , *via* the equations given in ref³¹. All fitting was performed using
35 Origin software (here we used Origin version 2015-2018) *via* the “Nonlinear Curve Fit”
36 function, according to equation 1. Care must be taken in fitting, with the best results obtained
37 by fitting the log of capacity *versus* rate as described in ref³¹. All fits and associated data are
38 given in the supplementary information. We note that the vast majority of published papers do
39 not give enough information to properly analyse rate data. While active material loading
40 (mg/cm^2) and proportions of active material *versus* binder and conductive additive are *usually*
41 given, electrode thickness is rarely explicitly mentioned in battery papers. This is unfortunate
42 as equation 2A makes clear that thickness has a critical impact on rate performance. In order
43 to facilitate rate analysis, we were forced to estimate electrode thickness in most cases (see SI).
44 We did this considering: A) the total mass loading and mass fraction of active material; B) the
45 densities of active material and binder/additive combination and C) the electrode porosity. The
46 parameters marked A are usually given in papers – where they are not, analysis is impossible.
47 The parameters marked B can almost always be estimated with reasonable accuracy. However,
48 the porosity (C) is very rarely given even though it is clearly critical for rate performance (as
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3 it impacts in ion diffusion in the electrolyte within the porous interior of the electrode). In most
4 cases, we were forced to estimate the porosity. Unless otherwise stated, we set the electrode
5 porosity at $P=0.5$. This is justifiable for 2D-based films as measurements have shown them to
6 have porosity close to this value.⁸² Assuming the actual porosity to lie in the range 0.4-0.6
7 yields a porosity error of 20%. Assuming the mass loading error is ~10% then yields an error
8 in electrode thickness of roughly 30% which is acceptable given the very broad range over
9 which L_E^2 / τ is distributed. We note that the set of papers surveyed, while considerable, cannot
10 be considered complete, simply as so many papers which report rate performance do not
11 provide enough information (as described above) to perform quantitative analysis.

12 The data sets in figures 3-5 representing a wide range of material types (labelled “all”) is taken
13 directly from ref³¹ and comprises the data labelled “cohort I, standard lithium ion electrodes”.

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ASSOCIATED CONTENT:

Supporting Information Available online: All capacity-rate fits, tabulated fit parameters, literature review tables, justification of values. This material is available free of charge *via* the Internet at <http://pubs.acs.org>.

No competing financial interests.

Figures

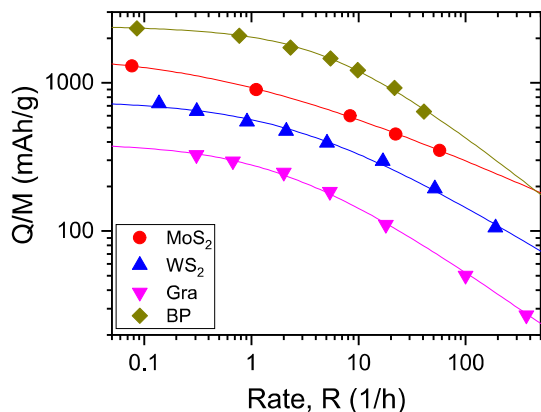


Figure 1: Examples of capacity *versus* rate data for battery electrodes based on 2D materials. The lines are fits to equation 1. Data are taken from the following papers: MoS₂¹⁸; WS₂²³; Graphene⁴⁵; black phosphorous¹⁰. All fits are shown in the SI.

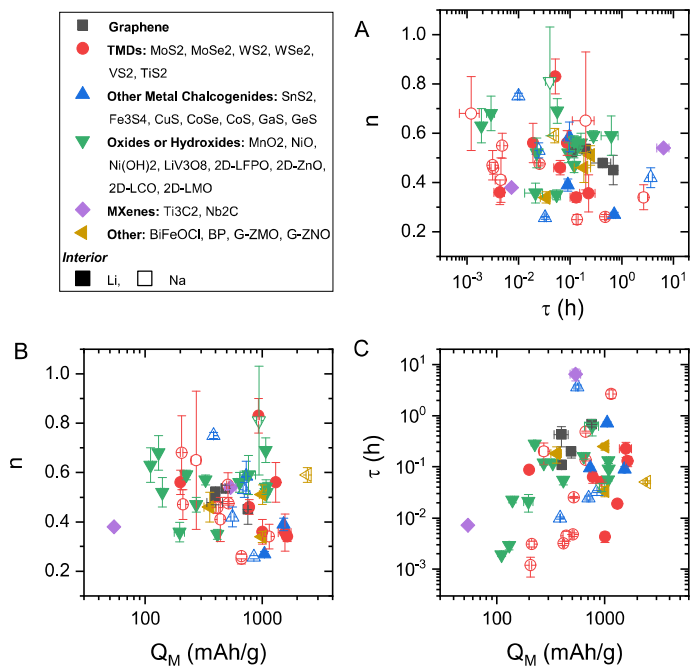


Figure 2: Fit parameters, obtained by fitting 48 data sets obtained from the literature (see SI, figures S1-4) to equation 1. These data sets encompass 25 different 2D materials grouped in the following families: graphene; transition metal dichalcogenides (TMDs); other metal chalcogenides, oxides or hydroxides, MXenes and other miscellaneous materials. The

individual materials making up the families are given in the legend. Closed symbols represent lithium ion batteries while open symbols represent sodium ion batteries. In A-C, these parameters are plotted against each other in three different combinations.

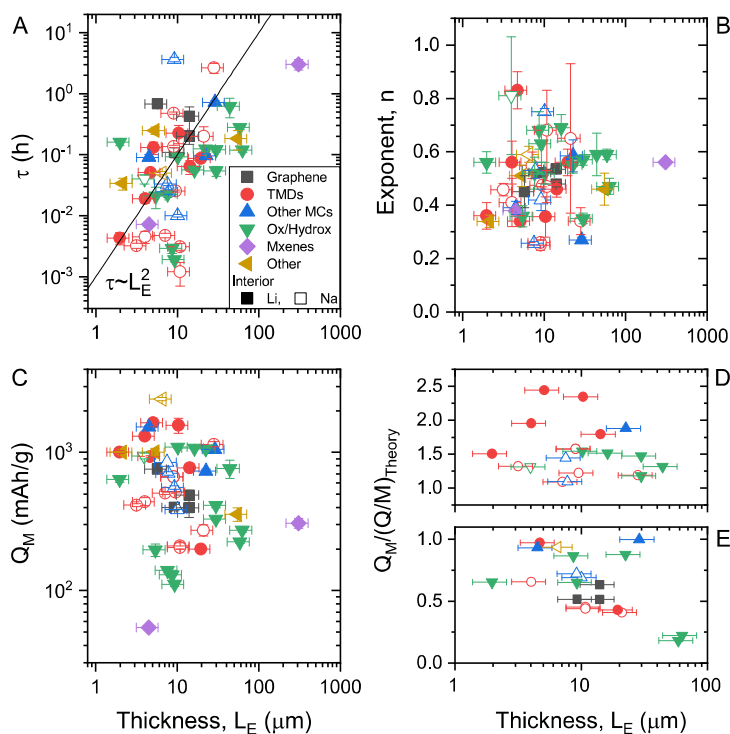


Figure 3: Thickness dependence of fit parameters. A-C) Thickness dependence of (A) time constant, τ , (B) exponent, n , and (C) low rate capacity, Q_M . D-E) Q_M normalised to theoretical specific capacity for (D) those materials showing anomalous behaviour ($Q_M > (Q/M)_{Theory}$) and (E) those materials showing normal behaviour ($Q_M \leq (Q/M)_{Theory}$). Closed symbols represent lithium ion batteries while open symbols represent sodium ion batteries. The legend in A applies to all panels.

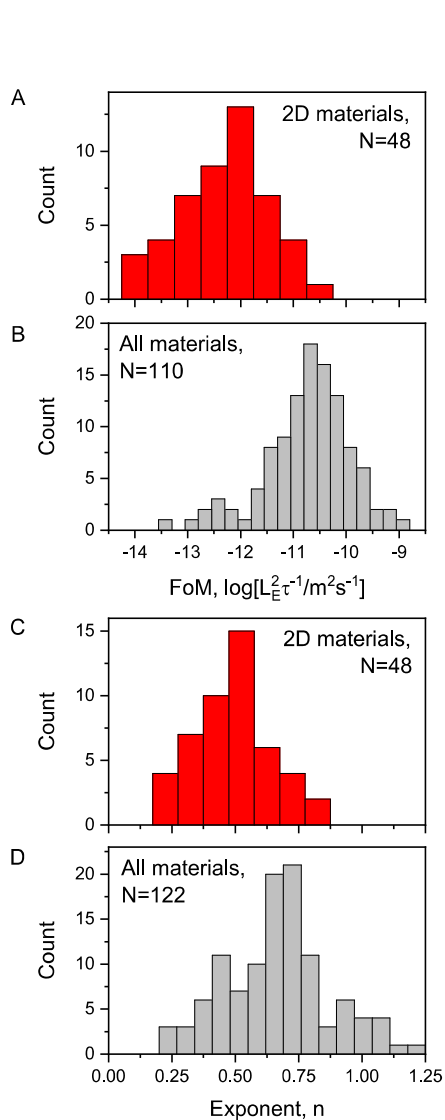


Figure 4: Histograms comparing the figure of merit for rate performance (A, B) and rate exponent (C, D) between 2D materials-based electrodes (A, C) and a wider data set including electrodes fabricated from many material types (B, D).

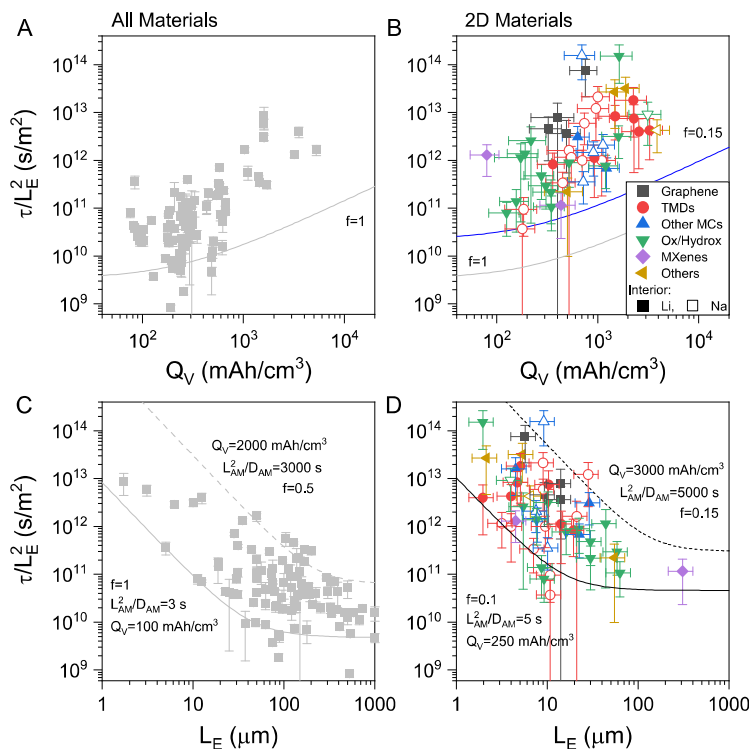
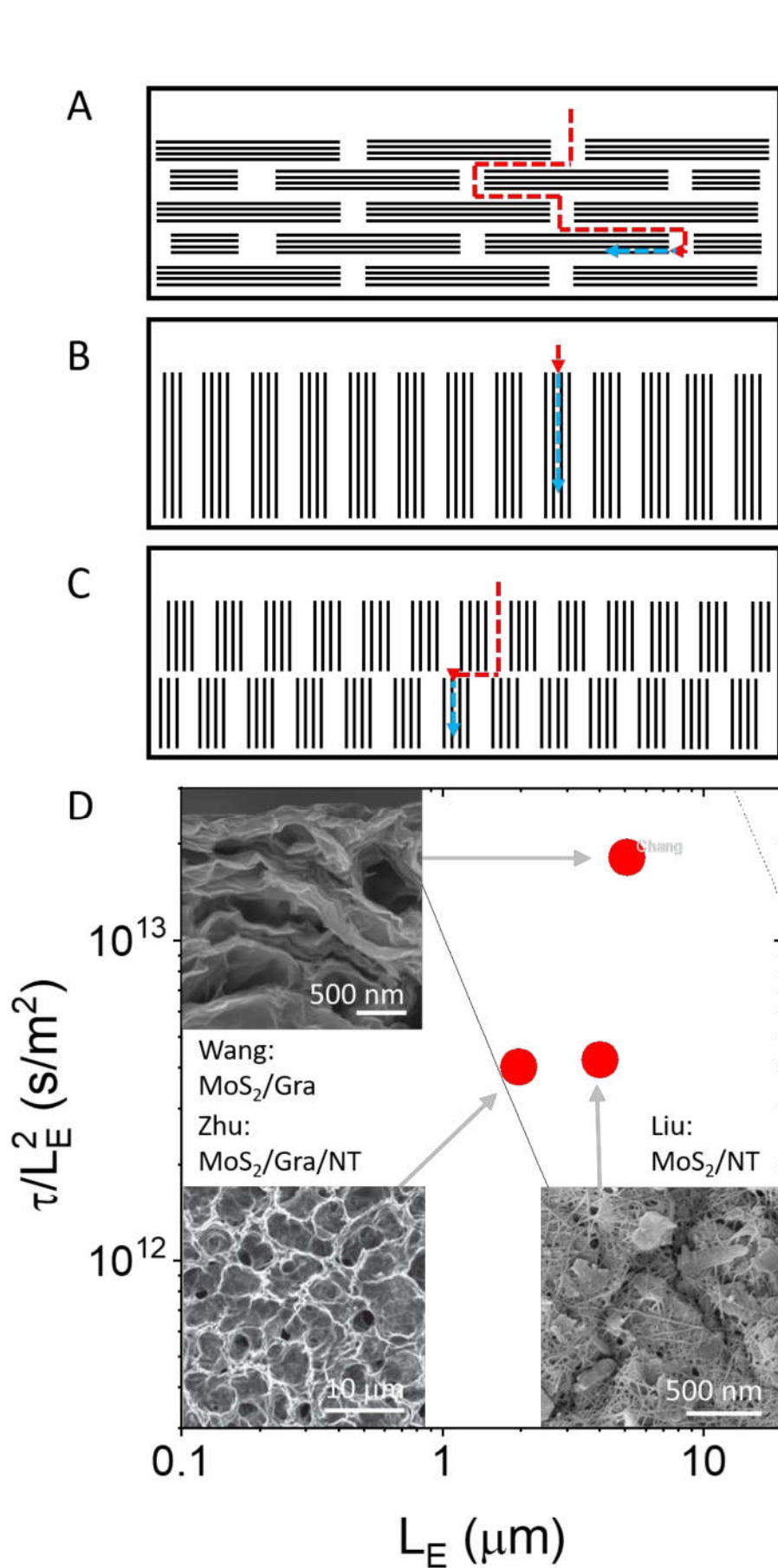


Figure 5: A-B) Time constant normalised to square of electrode thickness, τ / L_E^2 , plotted *versus* volumetric capacity of electrode, Q_V , for electrodes based on (A) “all materials” and (B) 2D materials. We note that τ / L_E^2 is the inverse of the figure of merit plotted in Figure 4 such that low values of τ / L_E^2 represent better rate performance. The lines in A-B are plots of equation 4 for $f=1$ (gray) and $f=0.15$ (blue), taking $L_S=25$ μ m, $\sigma_{BL}=\sigma_{P,S}=1$ S/m, $D_{BL}=3\times 10^{-10}$ m²/s. This equation simulates the lower limit of τ / L_E^2 , an approximation which is valid for thick electrodes or short diffusion times. Then, rate performance is limited only by ionic motion in the electrolyte within the porous interior of the electrode. The grey line in A-B represents the situation where ionic conductivity and diffusivity in the pores are equal to their values in bulk electrolyte. The blue line in (B) represent the situation when these parameters are reduced by a factor of $f=0.15$ relative to bulk liquid. C-D) Plots of τ / L_E^2 *versus* electrode thickness, L_E , for electrodes based on (C) “all materials” and (D) 2D materials. The lines represent upper (dashed) and lower (solid) limits of τ / L_E^2 for a given L_E . These were found by plotting equation 2b taking $P_S=0.5$, $\sigma_{BL}=1$ S/m, $D_{BL}=3\times 10^{-10}$ m²/s and using the parameters in the panels. N.B. the legend in B) also applies to D). Closed symbols represent lithium ion batteries while open symbols represent sodium ion batteries.

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Figure 6: A-C) Schematic illustrations of ion transport through nanosheet-based electrodes of three different morphologies: A) nanosheets aligned in plane; B) a single layer of vertically aligned nanosheets; C) multiple layers of vertically aligned nanosheets. Red dashed lines represent fast diffusion within electrolyte while blue arrows represent slower solid-state diffusion. D) Data from figure 5D reproduced for three Li-storing electrodes fabricated from MoS₂-based materials, as well as the plots of equation 2b. The insets show the morphology of each material and are used with permission.^{18, 41, 57} The top left image was reprinted with permission from Nano Energy 8, 183-195, copyright 2014 Elsevier. The bottom left image was reprinted with permission from Adv. Energy Mater. 5, 1401170, copyright 2014 Wiley.

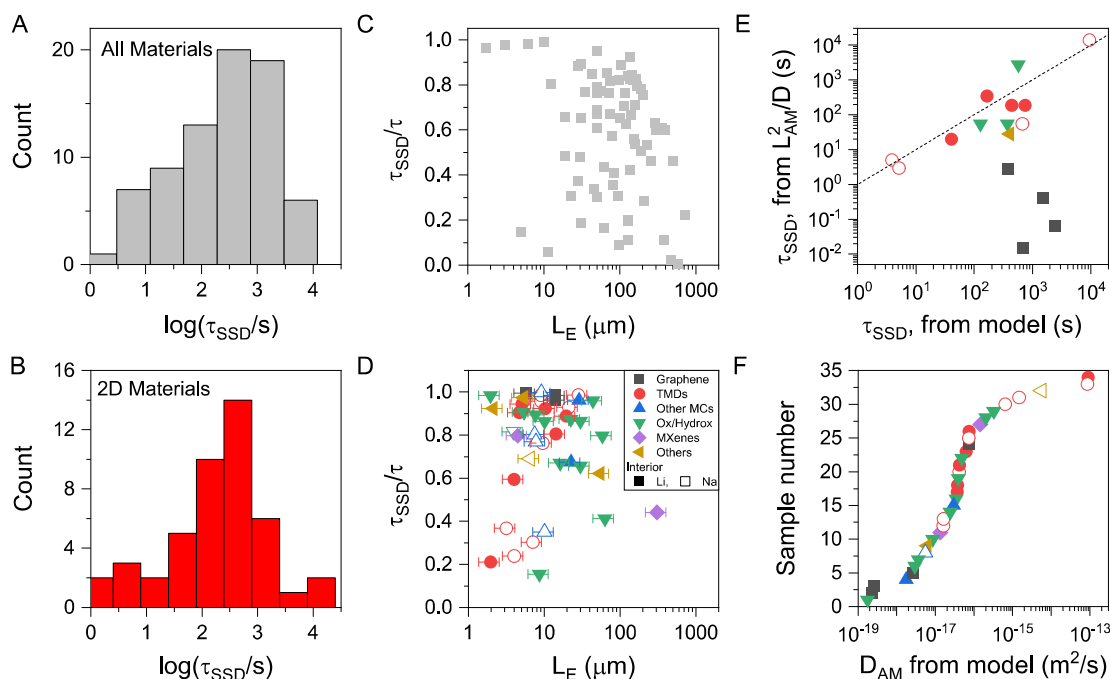
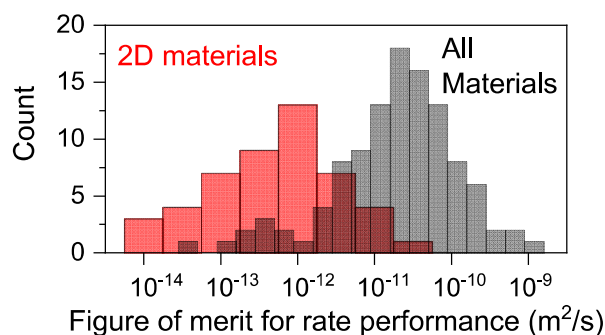


Figure 7: A-B) Histograms showing estimated solid-state diffusion time ($\tau_{SSD} = L_{AM}^2 / D_{AM}$) for "all materials" (A) and 2D materials (B). C-D) Ratio of solid-state diffusion time to time constant associated with charge/discharge for "all materials" (C) and 2D materials (D). E) Solid-state diffusion time for 2D materials found using the estimated particle size and the diffusion coefficient extracted from the literature plotted *versus* the extracted from model (using eq 5). The dashed line represents $y=x$. F) Solid-state diffusion coefficient of 2D materials extracted from τ_{SSD} (model) and the diffusion coefficient (literature) plotted in

ascending order. Plotted this way, this graph approximately represents the cumulative distribution of diffusion coefficients. N.B. the legend in D) also applies to E-F). Closed symbols represent lithium ion batteries while open symbols represent sodium ion batteries.

TOC



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