# On the Distortion of UWB Circularly Polarized Time-Domain Pulses in Presence of Rotation 

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#### Abstract

The paper provides a first theoretical study on the effect of rotational Doppler on circularly polarized pulsed communication. Despite the circularly polarized communication being considered immune to signal fading due to rotary misalignment, such misalignment will cause a frequency-invariant phase-shift. This phase shift will significantly distort the shape of the time-domain pulse. The property can be used for integration of orientation sensing into well establish pulse-based localization. However, it has also the potential to distort communication for some pulse-modulated UWB systems.


Keywords-Ultra-Wideband; UWB; Pulse modulation; Circular Polarization; Localization; Wireless sensing

## I. Introduction

Circularly Polarized (CP) antennas have been long used for communication between rotating objects (e.g. satellite communication, RFID) as they are immune to polarization losses due to misalignment [1]. In the presence of a rotation between transmitter and receiver antennas, the amplitude of the CP signal is not affected; however its phase will change proportionally to the rotation angle - a phenomena known as the rotational Doppler Effect [2]. A recent study demonstrated that the phenomena can be used to accurately measure rotational speeds of various devices, with very high dynamic range [3]. For instance: a rotating speed of 600M RPM (which was reported in [4] as the fastest man-made rotating object) would produce a frequency shift of 10 MHz , which falls well within measurement capabilities of state-of-the-art RF measurement equipment.

While the single-frequency signal allows measurement of rotating objects at a fixed-distance, it fails for more dynamic cases since the system cannot distinguish whether the phase shift originated from rotational or linear movement. However,


Fig. 1: $E_{x}$ and $E_{y}$ components of the CP Gaussian pulse: a) time-domain; b) amplitude of the spectrum; c) phase difference between $E_{x}$ and $E_{y}$ spectrum
contrary to the translational Doppler effect, the rotational case is frequency invariant, i.e. rotation by an angle $\alpha$ will produce a frequency shift of $\alpha$ at all frequencies (assuming the conditions for CP are satisfied) [5]. This property was used for dualfrequency implementation that allows simultaneous measurement of rotation and distance change [6]. However due to the lack of redundancy the technique was prone to errors.

This paper investigates for the first time the use of UltraWide Band (UWB) time-domain CP pulses [7] for measurement of the rotation. It provides a first theoretical study on how rotation influences the shape of UWB pulses and - most importantly - that such influence is significantly different from the one experienced by distance change. Since UWB pulses have been extensively used for accurate localization with <20 cm resolution [8], the implementation of rotation sensing based on the same technology is very attractive, due to easy integration capabilities.


Fig. 2: Investigated scenario

## II. Mathematical model

Fig. 1 demonstrates the two orthogonal components of a CP Gaussian pulse, representing frequencies from 3.2 to 6.2 GHz . This corresponds to the 3 dB Axial Ratio (AR) band of the antenna proposed in [9]. It was ensured that the spectrum of $E_{x}$ and $E_{y}$ components have the same amplitudes and are shifted in phase by $90^{\circ}$, thus providing an $\mathrm{AR}=0$ at all investigated frequencies.

Fig. 2 depicts the investigated scenario. The transmit antenna is an UWB CP antenna, transmitting the pulse with component $E_{x}$ and $E_{y}$. The receive antenna is dual linearlypolarized, measuring independently two orthogonal components $E_{p}$ and $E_{q}$, which lie in the plane orthogonal to the propagation direction of the pulse. The measured components $E_{p}$ and $E_{q}$ are rotated with respect to $E_{x}$ and $E_{y}$ by angle $\alpha$. This can be described as:

$$
\left[\begin{array}{l}
E_{p}  \tag{1}\\
E_{q}
\end{array}\right]=\left[\begin{array}{cc}
\cos \alpha & -\sin \alpha \\
\sin \alpha & \cos \alpha
\end{array}\right]\left[\begin{array}{l}
E_{x} \\
E_{y}
\end{array}\right]
$$

## III. Pulse distortion

Based on (1) the shape of the pulse was calculated for various rotations $\alpha$ in negative direction from $-60^{\circ}$ to $-360^{\circ}$ in $60^{\circ}$ steps. Fig. 3a shows the shape of the pulses received by the detector measuring the $E_{p}$ component, while Fig $3 \mathrm{~b}-E_{q}$ component. It can be seen, that the rotational Doppler Effect causes modulation which significantly changes pulse's shape. This distortion is unique to rotary movement and is significantly different from time-delay caused by distance travelled (used in localization applications) and from shortened/prolonged pulse due to the translational Doppler Effect. While facilitating simultaneous measurement of orientation and localization

This project has received funding from the European Union's Horizon 2020 program under the Marie Skłodowska-Curie Actions agreement No 713567 and from Science Foundation Ireland (SFI) grant No. 13/RC/2077.


Fig. 3: $E_{p}$ and $E_{q}$ components of received pulses as a function of $\alpha$
integrated into a single UWB tag, the demonstrated pulse distortion may also impede communication when certain pulsemodulation techniques are used on rotating platforms (e.g. pulsed satellite communication).

## IV. CONCLUSIONS

The paper demonstrates theoretically the impact of rotary movement on UWB CP pulse. It shows a significant distortion of such pulse, which is caused by a frequency-invariant phase shift due to rotational Doppler Effect.

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